

DATA STRUCTURES FOR IRRADIANCE ON THE SPHERE

ARTEFACTS AND REAL-TIME UPDATES

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Outline

- **The games industry**
- Introduction to game graphics
- Volume re-lighting
- Surface irradiance
- Summary

Games today

- Grand Theft Auto 5 (2013)
- 15.5 GB of data on 2 DVDs
- Team size > 1,000 people (!)
- Majority of these are artists
- Vast majority of the data is content (not code)
- GTA 5 made \$1bn in 48 hours (PS3 and Xbox 360 only)



Our target platforms



How do games get made?

- For a 'AAA' game there are three main ingredients:
 1. A large capital investment
 2. A huge number of artists
 3. A game engine
- This is a huge investment in technology

The engine

- Content pre-processor
- Content management
- Level editor
- Rendering
- Animation
- Physics
- Lighting baker
- AI
- Scripting
- ...



All integrated together

Video

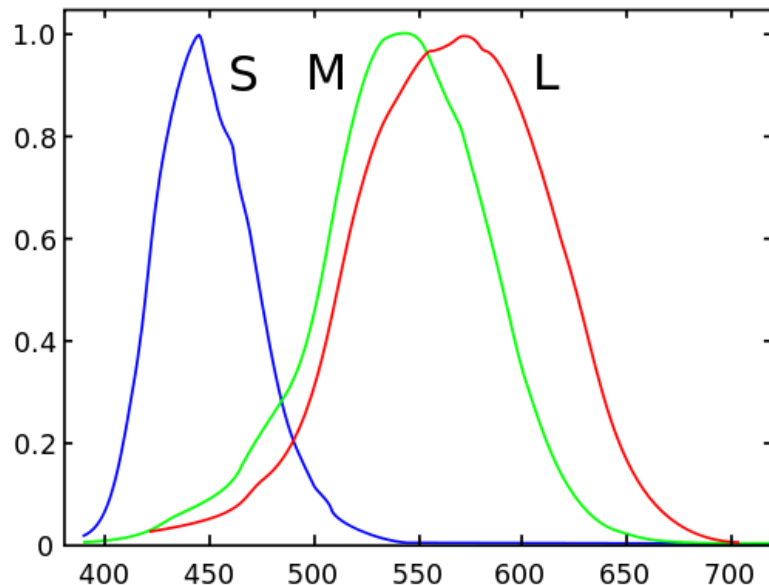


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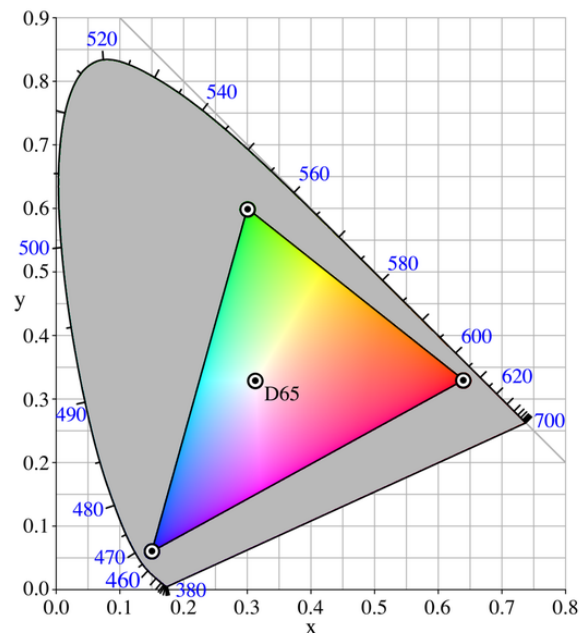
Simplification 1 – RGB Colour

- Restrict to three discrete colour channels
 - Don't work with entire spectrum – too hard!
- Motivated by physiology of human eye
 - Three types of cone cells: L, M, S [*]

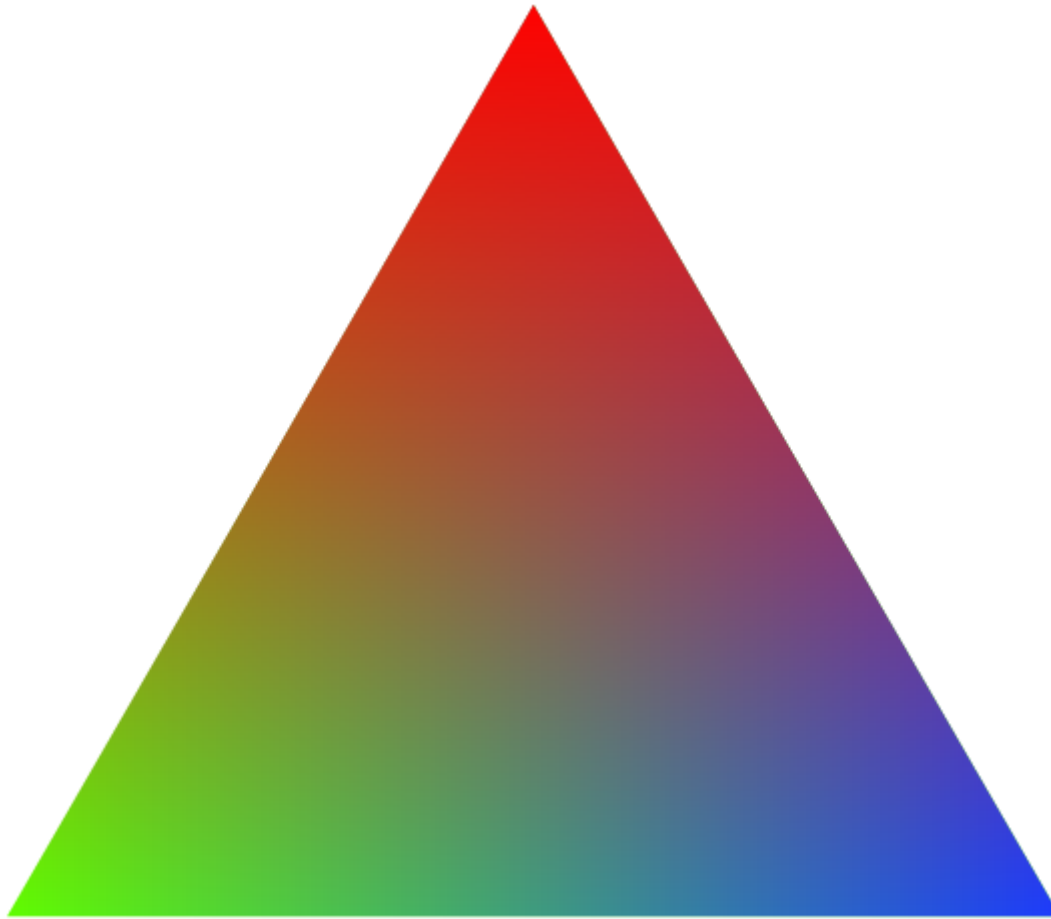


Drawbacks

- Hard to model some physical effects directly
 - Rainbows, polarisation, fluorescence, redshift
- Cannot reproduce all colours
 - Typically displays have this problem too

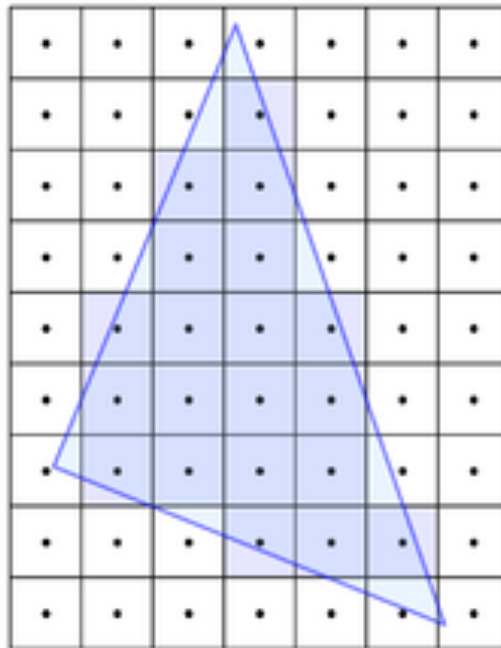


Simplification 2 – Triangles



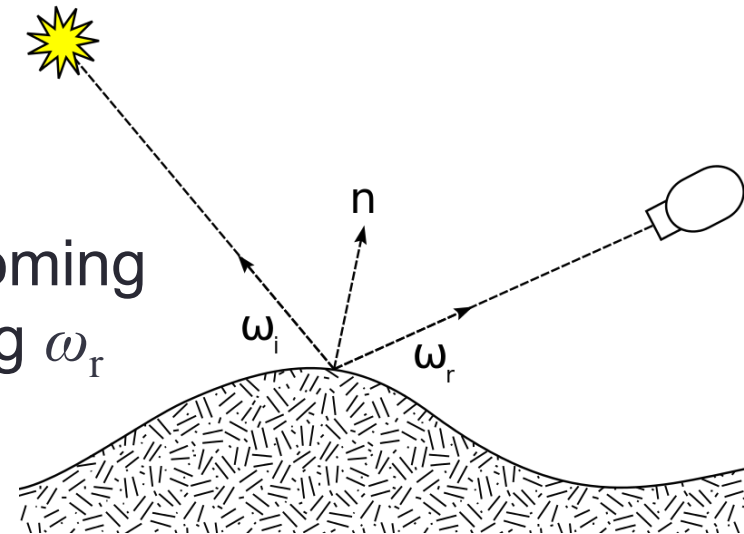
Simplification 3 – Rasterisation

- Single ray per pixel (more with MSAA)
- Give up depth-of-field blur as emergent property
- Add hardware for z-buffer, triangles 😊



Simplification 4 – BRDF

- Assume surfaces infinitesimally thin
- Disregard transmission
- Properties capture by a **Bidirectional Reflectance Distribution Function** for each surface
- Incoming light direction ω_i
- Outgoing light direction ω_r
- BRDF $f(\omega_i, \omega_r)$ is the ratio of the incoming light along ω_i which is reflected along ω_r



The Rendering Equation

$$L(\omega_r) = E(\omega_r) + \int_{\Omega} f(\omega_i, \omega_r) L_i(\omega_i) (\omega_i \cdot n) d\Omega_i$$

↑
outgoing light

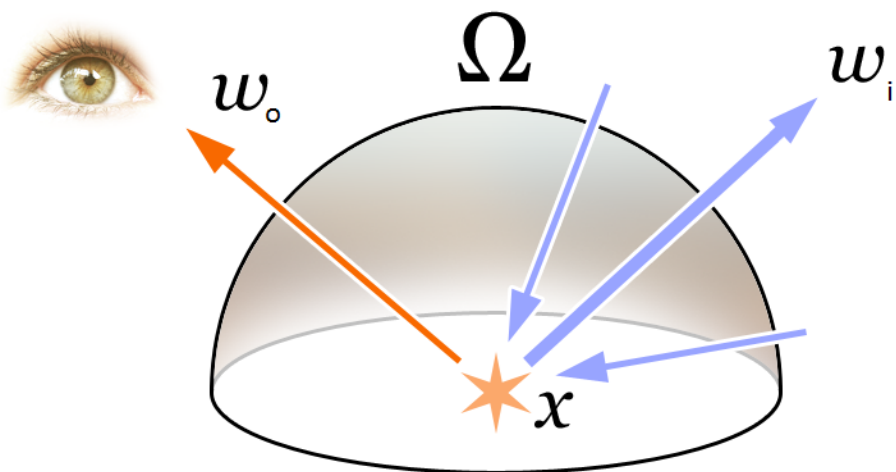
↑
emitted light

↑
BRDF

↑
incoming light

↑
integral over hemisphere

↑
incident angle term



Simplification 5 – Light Maps

- Simplest approach: use offline renderer
- Save result into a texture (“light map”)
- Index results with UV coordinates per vertex
- Look up results in shader – very fast
- Usually static – Enlighten computes these dynamically



Simplification 6 – Split BRDF

- BRDF = diffuse + specular
- Special case the specular term
- Bounce round the diffuse term - Radiosity
- This is a Lambertian diffuse surface
- Johann Heinrich Lambert, who was first to:
 - Prove pi is irrational
 - Use the term “albedo” in photometry
 - Prove formula for area of hyperbolic triangle

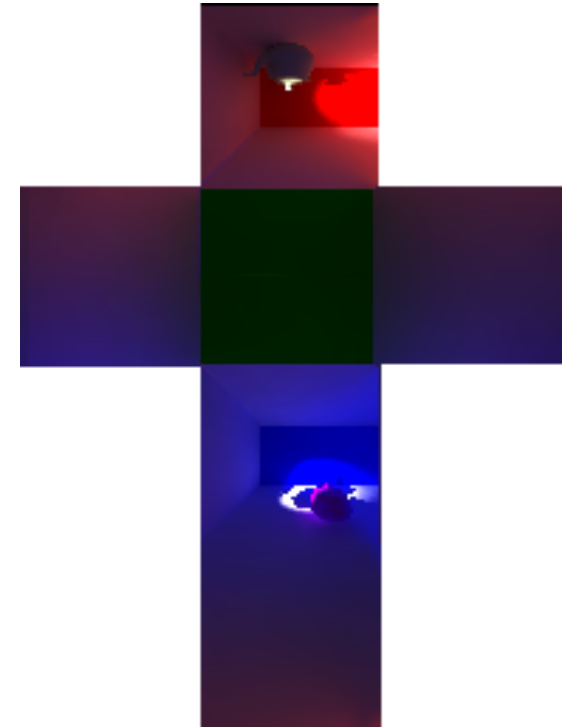
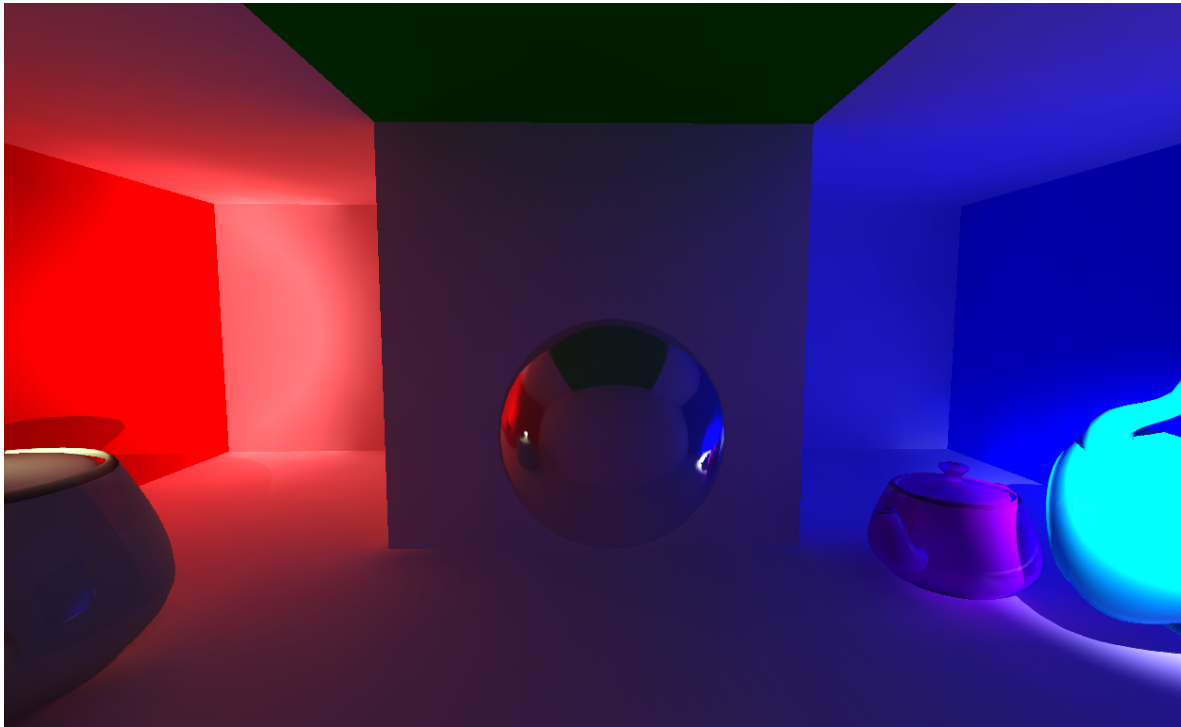


Albedo

$$L(\omega_r) = E(\omega_r) + \int_{\Omega} \frac{\alpha}{\pi} L_i(\omega_i) (\omega_i \cdot n) d\Omega_i$$

Simplification 7 – cube map specular

- Store a view of the scene in a cube map
- Efficient directional look-up
- Use mip-maps to blur based on roughness



Global illumination – example



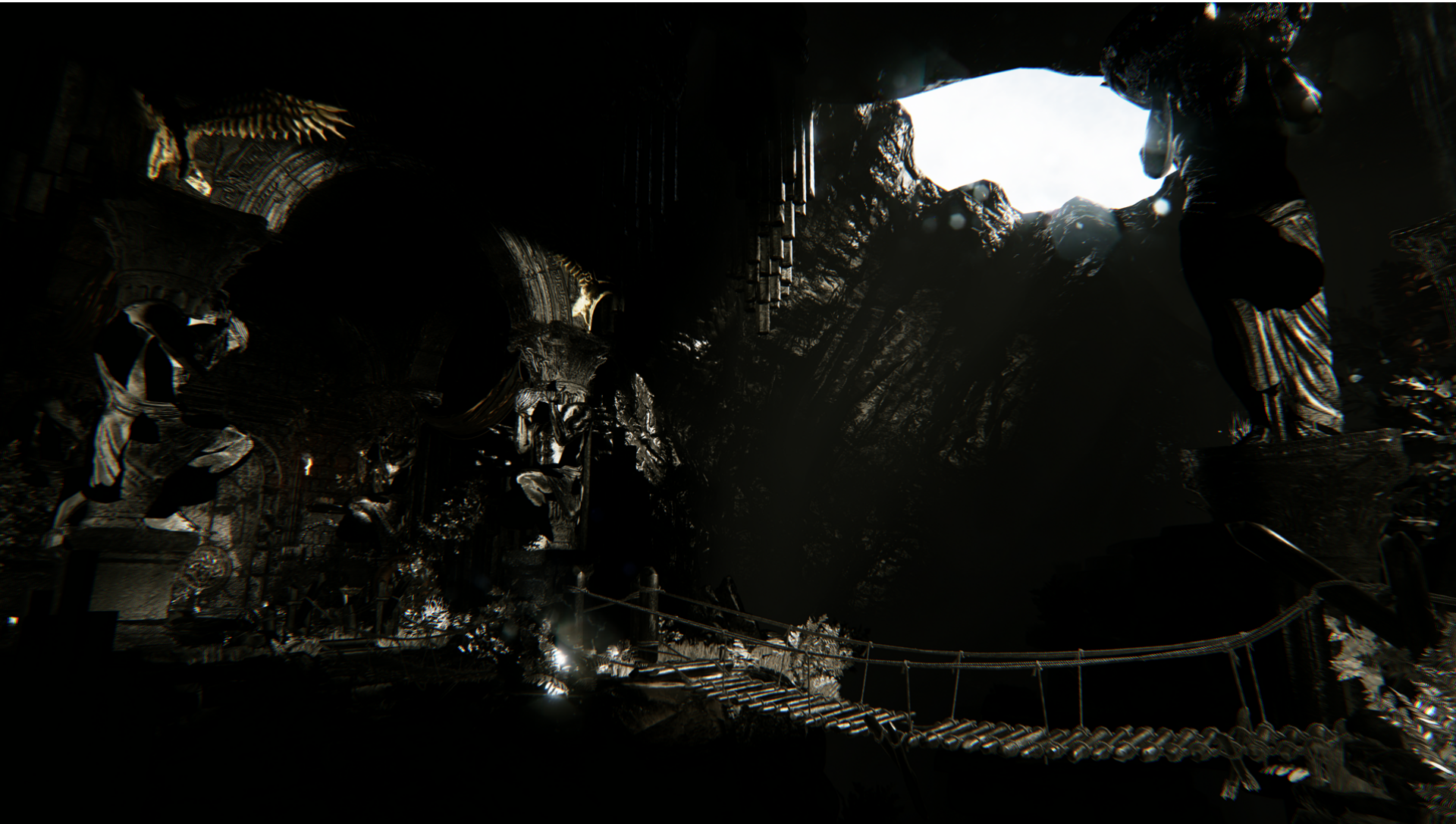
Global illumination – direct only



Global illumination radiosity pass



Global illumination – specular pass



Global illumination – final image



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Dynamic objects

- Small dynamic objects are lit with ‘light probes’
 - Capture the light field volumetrically
 - Relight geometry with arbitrary position/orientation
 - Use ‘spherical harmonics’



Some notation

- In graphics we rarely go beyond $l=2$
- Don't want to mess around with complex numbers
- Don't bother with factors of $\sqrt{\pi}$
- Normalise once
- Think of first three terms as scalar, vector, symmetric tensor

$$f(\boldsymbol{\omega}) = f_0 + \mathbf{f} \cdot \boldsymbol{\omega} + \boldsymbol{\omega}^t F \boldsymbol{\omega}$$

- In some cases makes sense to combine all 9 coefficients into a 3x3 matrix
 - Efficient for rotation

Useful result

- Ramamoorthi + Hanrahan 2001 (JOSA/A)
- At a probe, suppose the incoming light is given by

$$l(\boldsymbol{\omega}) = l_0 + \mathbf{l} \cdot \boldsymbol{\omega} + \boldsymbol{\omega}^t L \boldsymbol{\omega} + \dots$$

- The irradiance in a direction \mathbf{n} is given by

$$I(\mathbf{n}) = \int_H \frac{d\omega}{\pi} \boldsymbol{\omega} \cdot \mathbf{n} L(\boldsymbol{\omega})$$

- Which gives

$$I(\mathbf{n}) = l_0 + \frac{2}{3} \mathbf{l} \cdot \boldsymbol{\omega} + \frac{1}{4} \mathbf{n}^t L \mathbf{n} + \dots$$

Useful result

$$I(\boldsymbol{\omega}) = I_0 + \mathbf{l} \cdot \boldsymbol{\omega} + \boldsymbol{\omega}^t L \boldsymbol{\omega} + \dots$$

$$I(\mathbf{n}) = I_0 + \frac{2}{3} \mathbf{l} \cdot \boldsymbol{\omega} + \frac{1}{4} \mathbf{n}^t L \mathbf{n} + \dots$$

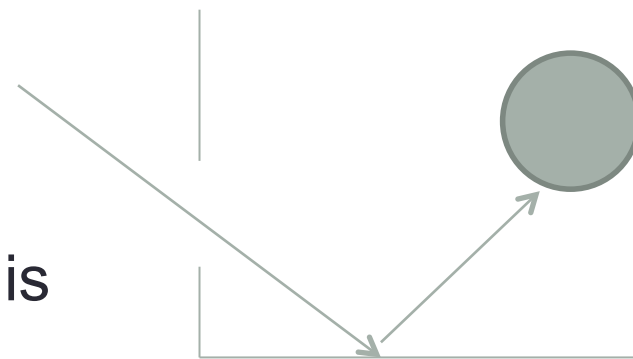
- All higher-order odd terms vanish from irradiance
- Coefficients of the even terms fall off as $1/l$
- Used to justify terminating at $l=2$
- On last generation consoles we just kept the scalar and vector terms!

Problems

- Low order harmonics produce some unpleasant artefacts
- Pool of light on floor from a window produces a highly directional input
- In this case the SH reconstruction can easily go negative
- In sampling terms

$$l = \frac{3}{n} \sum_a l^a \omega^a$$

- If one direction dominates then l is larger than scalar term



Problems

- Not clear that going to $l=2$ will resolve all problems
- May just introduce unpleasant ringing terms
- On latest games have a lot of objects lit with probes
 - Logic to determine which probes to compute is complex
 - Simpler to just update a voxel grid
 - Interpolate on the GPU
- End up computing quite a dense grid
 - 9 coefficients per colour channel = 27 in total
- Starting to look at multi-resolution techniques
 - Fill in the grid when data slowly changing
- But can we do better?

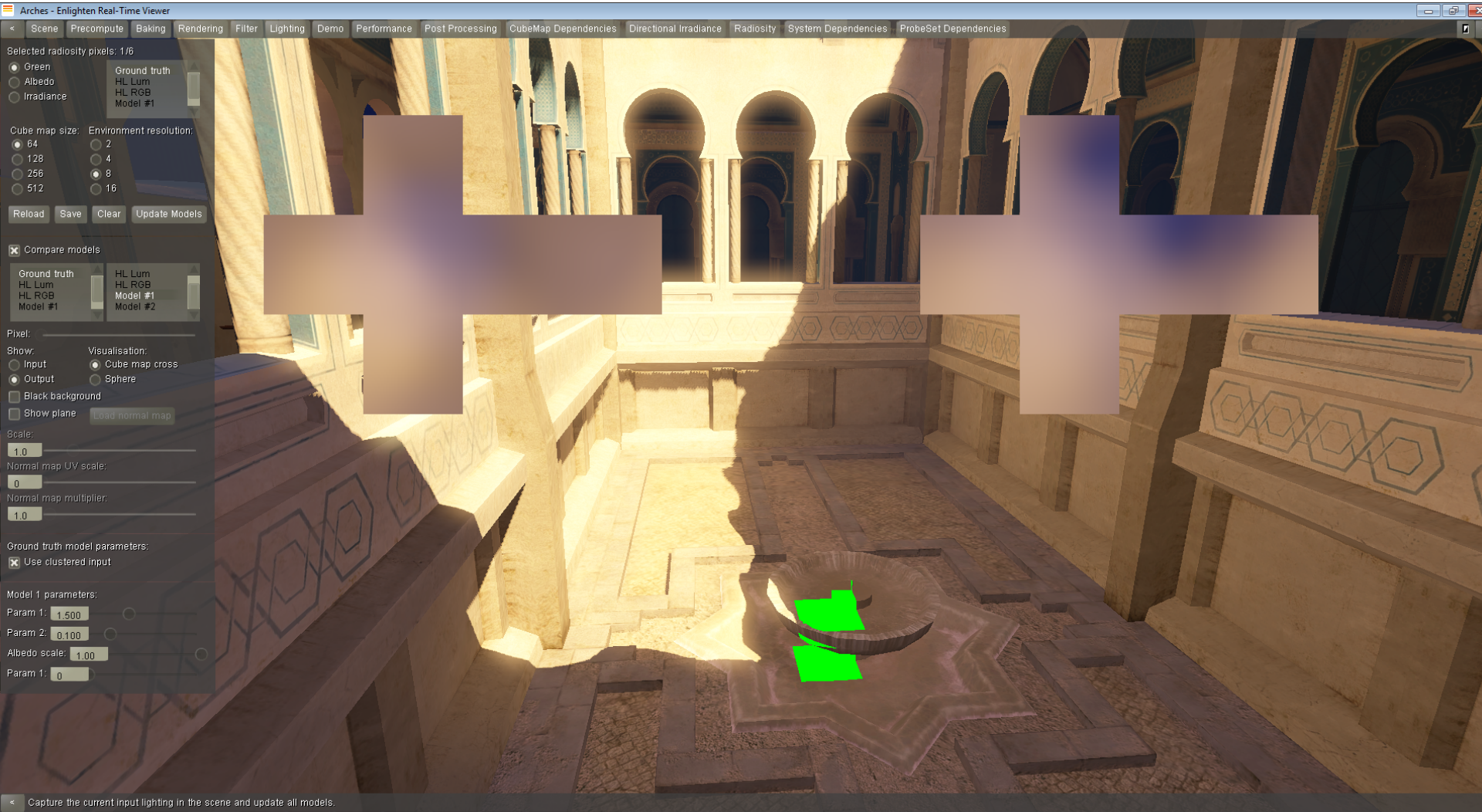
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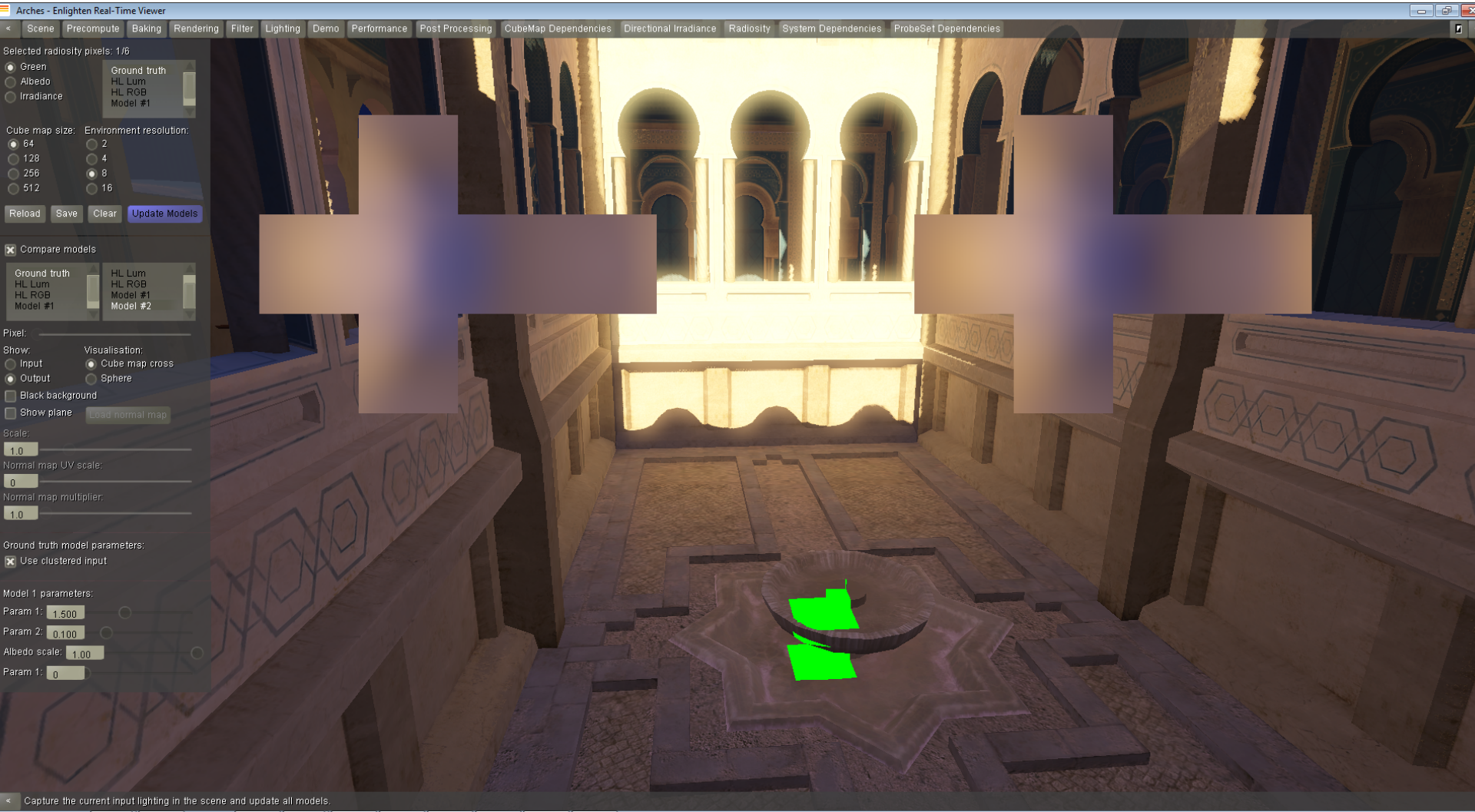
Surface Irradiance

- In Enlighten we compute the irradiance on surfaces at a low resolution
 - Fill in detail by upsampling
- Fine for smooth surfaces
- Need to consider geometric detail
 - Small artefacts on surface
 - Normal maps
- So we also compute an average direction of incoming light
- Do this under cosine distribution for simplicity
- Looking for a better model

Test scene



Test scene



Examples



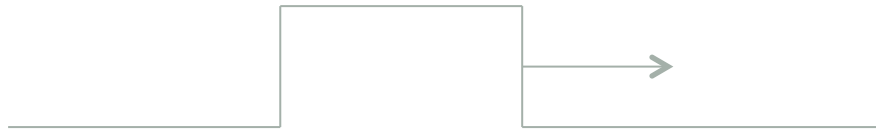
Problems

- Trying to deal with four types of geometry

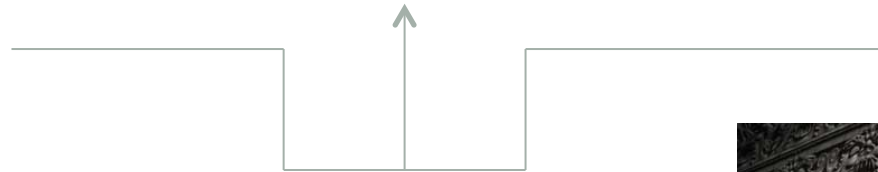
- Curved surfaces



- Extrusions



- Intrusions



- Normal maps



Problems

- Can reconstruct a plausible scalar + vector term:

$$I(\boldsymbol{\omega}) = L \frac{1}{2} (1 + \cos \theta) + (\mathbf{d} \wedge \mathbf{n}\mathbf{n}) \cdot \boldsymbol{\omega}$$

- But only so much you can do with a scalar and a vector
 - Raise a half-Lambert term to a power?
- Have to model the back reflections
- Have surface albedo information here
- Can try half Lambert in back direction

$$I'(\boldsymbol{\omega}) = L\alpha \frac{1}{2} (1 - \cos \theta)$$

Problems

- Given the measured data we can reconstruct a ‘best fit’ SH series (up to 2 usually)
- Often collect the directional information at lower resolution
- Want to collect directional data for separate light channels
- Directional data is very susceptible to quantization error
 - See this over a smooth curved surface
- Reconstruction will be done on the GPU in a shader
 - Has to be very simple and hardware friendly
- Can we use the fact the data is hemispherical more intelligently?

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Summary: wish list

- Want a spherical basis with
 - Small number of parameters
 - Smooth
 - Local support
 - Positive (functions are all positive)
 - Good rotation properties
 - Fast projection and reconstruction
 - Good interpolation and multi-resolution properties
- Want something similar for the hemisphere
- Also looking for compact representations of BRDF
 - Beyond Lambertian reflection
 - Blinn, Catmull Clark ...

Questions

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